

Objective: Know and use the rules of exponents to simplify radicals

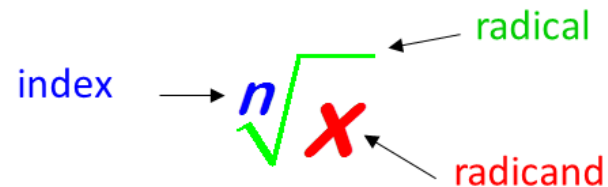
Concept

Rational and irrational numbers expressed in radical form can also be expressed with fractional exponents. When the number has a fractional exponent, it is said to be in [rational exponent](#) form.

$$\sqrt[n]{b} = b^{\frac{1}{n}}$$

and

$$\sqrt[n]{b^p} = b^{\frac{p}{n}} \text{ or } (\sqrt[n]{b})^p = b^{\frac{p}{n}}$$



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Ex) Write the expression in radical form.

$$5^{\frac{2}{3}}$$

*← exponent*  
*← exponential form*  
*← index*

$$\sqrt[3]{5^2}$$

~~$$\sqrt[3]{5}$$~~

$$= \boxed{\sqrt[3]{25}}$$

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Ex) Write the radical using rational exponents.

$$\overset{\text{denominator}}{\curvearrowright} 5 \sqrt[4]{3} \overset{\text{numerator}}{\curvearrowleft} \quad \leftarrow \text{radical form}$$

$$= \boxed{4^{\frac{3}{5}}} \quad \text{exponent form}$$

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Concept

Negative Exponent Rule:  $x^{-n} = \frac{1}{x^n}$  or  $\frac{1}{x^{-n}} = x^n$

Product of Powers:  $(x^n) \cdot (x^m) = x^{n+m}$

Power of a Power:  $(x^n)^m = x^{n \cdot m}$

Quotient of Powers:  $\frac{x^n}{x^m} = \frac{x^{n-m}}{1} = x^{n-m}$  or  $\frac{x^n}{x^m} = \frac{1}{x^{m-n}}$

Zero Exponent Rule:  $x^0 = 1$

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Ex) Evaluate each expression. Show your work.

$$32^{\frac{2}{5}}$$

2 exponent  
5 ← index

①  $(\sqrt[5]{32})^{-2}$

$(2)^{-2}$

$= \frac{1}{2^2}$

$= \boxed{\frac{1}{4}}$

★ use negative exponent rule

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Ex) Evaluate each expression. Show your work.

$$125^{-\frac{1}{3}} \cdot 125^{\frac{2}{3}}$$

$$\textcircled{1} = 125^{-\frac{1}{3} + \frac{2}{3}}$$

$$= 125^{\frac{1}{3} \text{ exp. index}}$$

$$\textcircled{2} \sqrt[3]{125^1} = \sqrt[3]{125} = \boxed{5}$$

$$\star (x^n) \cdot (x^m) = x^{n+m}$$

$$(x^n)^m = x^{n \cdot m}$$

$$\frac{x^n}{x^m} = \frac{x^{n-m}}{1} = x^{n-m}$$

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Ex) Evaluate each expression. Show your work.

$$\begin{aligned} & \left(32^{\frac{4}{3}}\right)^{\frac{3}{5}} \\ \textcircled{1} & 32^{\frac{4}{3} \cdot \frac{3}{5}} \\ & = 32^{\frac{12}{15}} \text{ reduce} \\ & = 32^{\frac{4}{5}} \end{aligned}$$

$$\textcircled{2} \left(\sqrt[5]{32}\right)^4 = 2^4 = \boxed{16}$$

$$(x^n) \cdot (x^m) = x^{n+m}$$

$$\star (x^n)^m = x^{n \cdot m}$$

$$\frac{x^n}{x^m} = \frac{x^{n-m}}{1} = x^{n-m}$$

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Ex) Evaluate each expression. Show your work.

$$\left(\frac{4}{25}\right)^{\frac{3}{2}}$$

$$(x^n) \cdot (x^m) = x^{n+m}$$

$$\star (x^n)^m = x^{n \cdot m}$$

$$\frac{x^n}{x^m} = \frac{x^{n-m}}{1} = x^{n-m}$$

$$\textcircled{1} \left(\frac{4}{25}\right)^{\frac{3}{2}}$$

$$\frac{4^{1 \cdot \frac{3}{2}}}{25^{1 \cdot \frac{3}{2}}} = \frac{4^{\frac{3}{2} \text{ exp}}}{25^{\frac{3}{2} \text{ exp}}}$$

$$\textcircled{2} \frac{(\sqrt{4})^3}{(\sqrt{25})^3} = \frac{2^3}{5^3} = \boxed{\frac{8}{125}}$$





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Ex) Evaluate each expression. Show your work.

$$\frac{25^{\frac{5}{8}}}{25^{\frac{1}{8}}}$$

①  $25^{\frac{5}{8} - \frac{1}{8}}$   
 $= 25^{\frac{4}{8}}$  reduce  
 $= 25^{\frac{1}{2}}$

②  $\sqrt{25^1} = \sqrt{25} = \boxed{5}$

$$(x^n) \cdot (x^m) = x^{n+m}$$

$$(x^n)^m = x^{n \cdot m}$$

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$$\star \frac{x^n}{x^m} = \frac{x^{n-m}}{1} = x^{n-m}$$



Objective: Know and use the rules of exponents to simplify radicals

Ex) Evaluate each expression. Show your work.

$$36^{\frac{4}{3}} \cdot 36^{\frac{1}{6}}$$

$$\textcircled{1} \quad 36^{\frac{2 \cdot 4}{2 \cdot 3} + \frac{1}{6}}$$

$$= 36^{\frac{8}{6} + \frac{1}{6}}$$

$$= 36^{\frac{9}{6}} \text{ reduce}$$

$$= 36^{\frac{3}{2}}$$

$$\textcircled{2} \quad (\sqrt{36})^3 = 6^3$$
$$= \boxed{216}$$

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Ex) Evaluate each expression. Show your work.

$$\frac{16^{\frac{3}{2}}}{16^{\frac{1}{4}}}$$

$$\textcircled{1} \quad \frac{2 \cdot 3}{2 \cdot 2} - \frac{1}{4}$$

$$= 16^{\frac{6}{4} - \frac{1}{4}}$$

$$= 16^{\frac{5}{4}}$$

$$\textcircled{2} \quad (\sqrt[4]{16})^5 = 2^5 = \boxed{32}$$

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Closure

Explain the different meanings of the numerator and denominator of the expression. What is the value of the expression?

$$64^{\frac{2}{3}}$$

The denominator of 3 represents the cube root of the base of 64. The numerator of 2 represents the power on the cube root of 64. The value of the expression is 16.

