

Objective: Model situations with factors of polynomials and use them to solve problems.

Ex) The area of a rectangular wheat field can be modeled by $15x^2 - 2x - 24$ square meters.



a) Find the expressions of x that could represent the dimensions of the field.

Area = length · width

$15x \cdot x$
 $3x \cdot 5x$ ↓ $m^2 = m \cdot m$
 $15x^2 - 2x - 24 = (3x - 4)(5x + 6)$

$(3x - 4)(5x + 6)$

Conclusion: The dimensions of the field can be represented by $(3x - 4)$ meters and $(5x + 6)$ meters.

b) If the value of x is 20, what are the dimensions of the field?

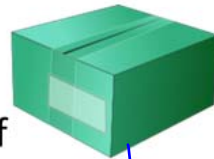
$(3x - 4)$ meters } $(5x + 6)$ meters
 $3(20) - 4$ } $5(20) + 6$
 $60 - 4$ } $100 + 6$
 56 meters } 106 meters

The dimensions of the field, if $x = 20$, are 56 meters and 106 meters.

Objective: Model situations with factors of polynomials and use them to solve problems.

Ex) The volume of a shipping box is modeled by $2x^3 - 7x^2 - 4x$ cubic inches.

a) Find the expressions of x that could represent the length, width, and height of the box.



rectangular prism

b) If the value of x is 15, what are the dimensions of the box?

$$\text{in}^3 = \text{in} \cdot \text{in} \cdot \text{in}$$

$$\text{volume} = \text{length} \cdot \text{width} \cdot \text{height}$$

$$2x^3 - 7x^2 - 4x = x(2x+1)(x-4)$$

$$x(2x^2 - 7x - 4)$$

$$x(2x+1)(x-4)$$

conclusion

The length, width, and height of the shipping box can be represented by x inches, $(2x+1)$ inches, and $(x-4)$ inches.

$$x \text{ in} \rightarrow 15 \text{ in}$$

$$(2x+1) \text{ in} \rightarrow 31 \text{ in}$$

$$2 \cdot 15 + 1$$

$$(x-4) \text{ in} \rightarrow 11 \text{ in}$$

$$15 - 4$$

The dimensions of the shipping box, if $x=15$, are 15 in, 31 in, and 11 in.

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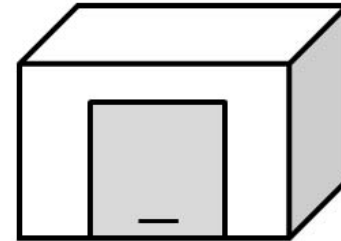
Practice) The volume of a rectangular storage shed is modeled by the polynomial $2x^3 + 9x^2 - 35x$ cubic feet.

a) Write expressions of x that could be used to represent the dimensions of the shed.

$$V = l \cdot w \cdot h$$

The dimensions of the shed can be represented by x feet, $(2x - 5)$ feet, and $(x + 7)$ feet.

$$\begin{aligned} V &= 2x^3 + 9x^2 - 35x \\ &= x(2x^2 + 9x - 35) \\ &= x(2x - 5)(x + 7) \end{aligned}$$



b) If $x = 10$, what are the dimensions of the shed?

$$x = 10$$

$$10 \text{ ft}$$

$$(2(10) - 5) = 20 - 5 = 15 \text{ ft}$$

$$((10) + 7) = 17 \text{ ft} \quad \text{If } x = 10, \text{ the dimensions of the shed are } 10 \text{ ft, } 15 \text{ ft, and } 17 \text{ ft.}$$

c) Penny is planning on renting a storage shed. She's determined that she needs a storage volume of 2000 cubic feet. Is this storage shed large enough to meet Penny's needs? Explain your reasoning.

$$V = l \cdot w \cdot h = 10 \text{ ft} \cdot 15 \text{ ft} \cdot 17 \text{ ft} = 2550 \text{ ft}^3$$

Yes, the storage shed is large enough because its volume is 2550 cubic feet, which is 550 cubic feet larger than Penny needs.

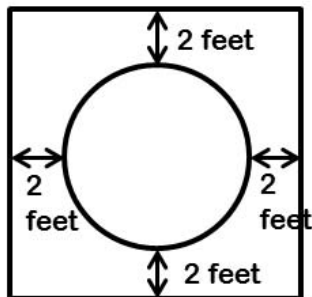


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Practice) A circular fountain is set within a square flower garden as shown.

The area of the flower garden is $16x^2 + 24x + 9$ square feet.

a) Write expressions of x to model the sides of the flower garden.



$$A = l \cdot w$$

$$A = 16x^2 + 24x + 9$$

$$= (4x + 3)(4x + 3)$$

The sides of the flower garden can be modeled by $(4x + 3)$ feet and $(4x + 3)$ feet.

b) What is the diameter of the fountain as an expression of x ?

diameter = side length - garden on edges

$$(4x + 3) \text{ ft} - 4 \text{ ft} = (4x - 1) \text{ ft}$$

The diameter of the fountain is $(4x - 1)$ feet.

c) If $x = 3$, what is the diameter of the fountain?

$$\text{diameter} = 4(3) - 1 \text{ ft} = 12 - 1 = 11 \text{ ft}$$

If $x = 3$, the diameter of the fountain is 11 feet.

d) If $x = 3$, what is the perimeter of the flower garden?

$$\text{one side} = 4x + 3 \text{ ft}$$

$$\text{one side} = 4(3) + 3 = 12 + 3 = 15 \text{ ft}$$

$$\text{A square has four equal sides. Perimeter} = 4 \cdot 15 \text{ ft} = 60 \text{ ft}$$

If $x = 3$, the perimeter of the flower garden is 60 feet.