

Objective: Model Real World Situations with Polynomials

Ex) The data from the U.S. Census Bureau for 2005-2009 shows that the number of male students (in thousands) enrolled in high school in the United States can be modeled by the function $M(x) = -10.4x^3 + 74x^2 - 3.4x + 8320.2$, where x is the number of years after 2005. The number of female students (in thousands) enrolled in high school in the United States can be modeled by the function $F(x) = -13.8x^3 + 55.3x^2 + 141x + 7880$, where x is the number of years after 2005.

a) Write a new function, $T(x)$, that models the total number of students in thousands after 2005. $T(x) = M(x) + F(x)$

$$\begin{aligned} M(x) &= -10.4x^3 + 74x^2 - 3.4x + 8320.2 \\ + F(x) &= -13.8x^3 + 55.3x^2 + 141x + 7880 \\ \hline T(x) &= -24.2x^3 + 129.3x^2 + 137.6x + 16,200.2 \end{aligned}$$

b) Estimate the total number of students enrolled in high school in the United States in 2009. $x = 2009 - 2005$

$$x = 4$$

$$\begin{aligned} T(4) &= -24.2(4)^3 + 129.3(4)^2 + 137.6(4) + 16,200.2 \\ &\quad \times 1000 \\ &= 17,270,600 \end{aligned}$$

conclusion

In 2009 there were about 17,270,600 students enrolled in high school in the United States.

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Ex) From 1995 through 2010, the yearly gross revenue (in millions) for a candy company can be modeled by the function $R(t) = 0.01t^3 - 0.2677t^2 + 1.7779t + 2.1805$ and the yearly cost (in millions) can be modeled by the function $C(t) = 0.0008t^3 - 0.0096t^2 + 0.0288t + 2.4$ where t is the number of years since 1995.

a. Write a new function, $P(t)$, that models the yearly profit after 1995.

$$P(t) = R(t) - C(t) \quad \text{profit} = \text{revenue} - \text{costs}$$

$$P(t) = (0.01t^3 - 0.2677t^2 + 1.7779t + 2.1805) + (-0.0008t^3 + 0.0096t^2 + 0.0288t + 2.4)$$

$$P(t) = 0.0092t^3 - 0.2581t^2 + 1.7491t - 0.2195$$

b. What was the total profit the candy company had in 2007?

$$\hookrightarrow t = 2007 - 1995 = 12$$

$$P(12) = 0.0092(12)^3 - 0.2581(12)^2 + 1.7491(12) - 0.2195$$

$$\times 1,000,000$$

$$= \$-499,100 \text{ (loss of } \$499,100)$$

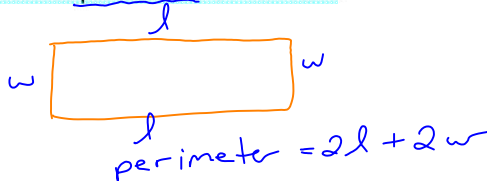
conclusion

In 2007 the candy company had a loss of \$499,100.

Objective: Model Real World Situations with Polynomials

Ex) A straight section of a biking path has a width, in feet, modeled by the function $W(x) = 2x + 7$ and a length, in feet, modeled by the function $L(x) = x^3 + 4x^2 + 5x - 6$.

a) Write a new function, $P(x)$, that represents the perimeter of the bike path section.

$$\begin{aligned}
 P(x) &= 2 \cdot L(x) + 2 \cdot W(x) \\
 &= 2(x^3 + 4x^2 + 5x - 6) + 2(2x + 7) \\
 &= 2x^3 + 8x^2 + 10x - 12 + 4x + 14 \\
 P(x) &= 2x^3 + 8x^2 + 14x + 2
 \end{aligned}$$


b) Find the perimeter of the described section of the biking path if the width is 17 feet.

$$\begin{aligned}
 \textcircled{1} \text{ width } w(x) &= 2x + 7 \\
 \downarrow \\
 17 &= 2x + 7 \\
 -7 &\quad -7 \\
 \hline
 10 &= 2x \\
 \frac{10}{2} &= \frac{2x}{2} \\
 x &= 5
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{2} \quad P(5) &= 2(5)^3 + 8(5)^2 + 14(5) + 2 \\
 &= 522 \text{ feet}
 \end{aligned}$$

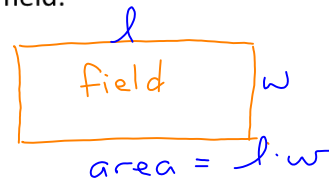
$\textcircled{3}$ The section of the biking path has a perimeter of 522 feet.

Objective: Model Real World Situations with Polynomials

Ex) A farmer has a field he needs to mow before he can plant wheat. The length of the field can be modeled by $L(x) = 5x^3 + 2x^2 + 7$ feet and the width of the field can be modeled by $W(x) = 3x^2 - 4x + 2$ feet.

a) Write a function, $A(x)$, that models the area of the field.

$$A(x) = L(x) \cdot W(x)$$



$$A(x) = (5x^3 + 2x^2 + 7)(3x^2 - 4x + 2)$$

$$= 5x^3(3x^2 - 4x + 2) + 2x^2(3x^2 - 4x + 2) + 7(3x^2 - 4x + 2)$$

$$= 15x^5 - 20x^4 + 10x^3 + 6x^4 - 8x^3 + 4x^2 + 21x^2 - 28x + 14$$

$$A(x) = 15x^5 - 14x^4 + 2x^3 + 25x^2 - 28x + 14$$

b) The farmer can mow the field at a rate of 1000 square feet per minute. If the value of x is 8, how long, to the nearest hour, will it take the farmer to mow the field?

$$x = 8 \quad \textcircled{1} \quad A(8) = 15(8)^5 - 14(8)^4 + 2(8)^3 + 25(8)^2 - 28(8) + 14$$

$$= 436,590 \text{ ft}^2$$

$$\textcircled{2} \quad \frac{436,590 \text{ ft}^2}{1} \cdot \frac{1 \text{ min}}{1000 \text{ ft}^2} \cdot \frac{1 \text{ hr}}{60 \text{ min}}$$

≈ 7 hours

$\textcircled{3}$ It will take the farmer about 7 hours to mow the field.