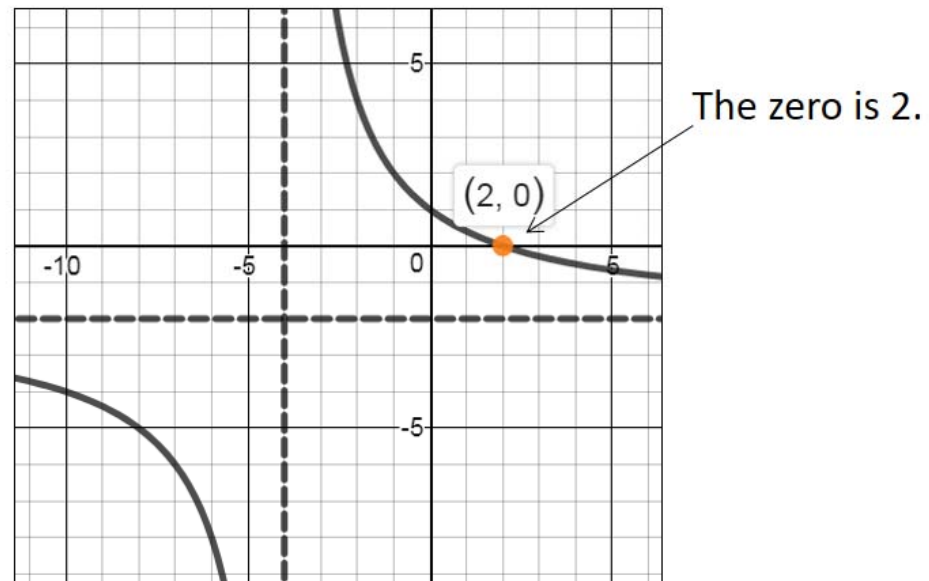


Objective: Determine key features of a rational function from its graph

Concept

Zeros: The **zero of a function** is a **value of x** that makes the value of a function equal to zero.



Objective: Determine key features of a rational function from its graph

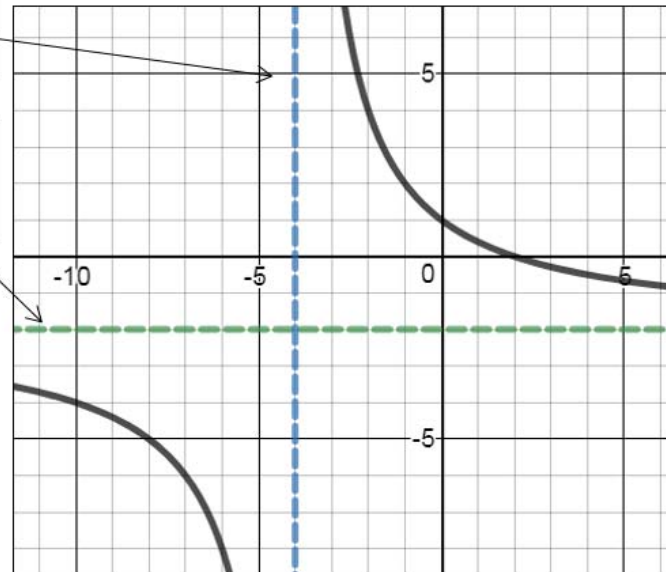
Concept

Asymptote: An asymptote is a line that the graph of a function approaches but never touches as the value of x approaches positive or negative infinity.

Rational functions contain both **vertical asymptotes** and **horizontal asymptotes**. Asymptotes are visually represented by **dashed** lines.

vertical asymptote
 $x = -4$

horizontal asymptote
 $y = -2$



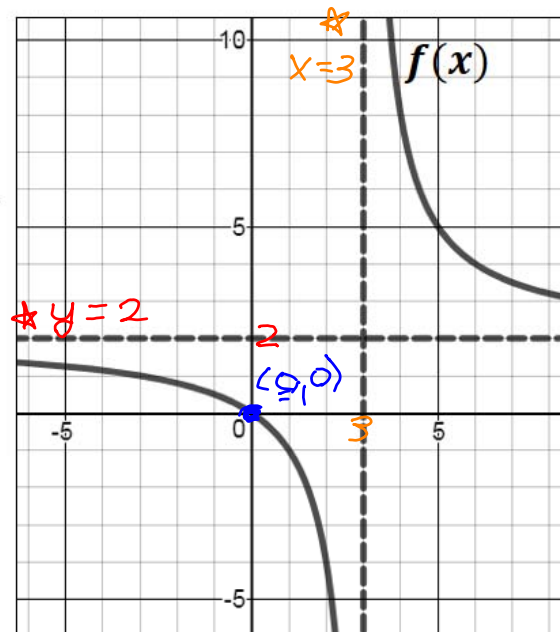
Objective: Determine key features of a rational function from its graph

Ex) Determine the key features for the function $f(x)$.

The zero(s) are at 0.

The vertical asymptote is $x = 3$

The horizontal asymptote is $y = 2$



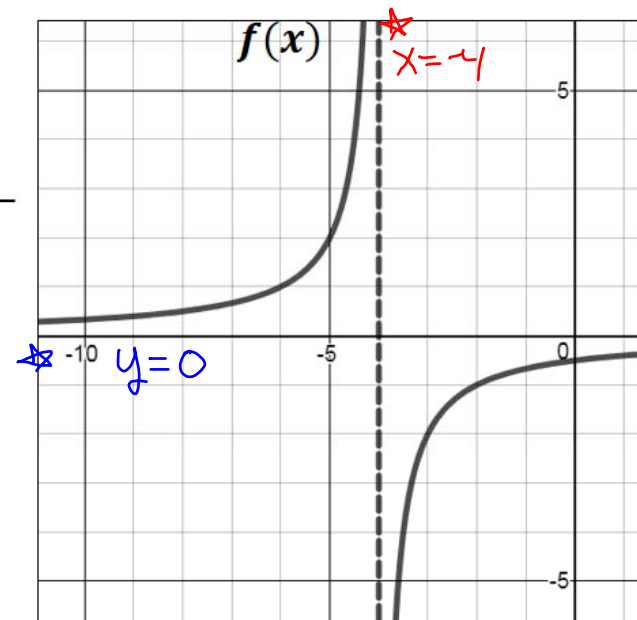
Objective: Determine key features of a rational function from its graph

Ex) Determine the key features for the function $f(x)$.

The zero(s) are at no zeros.

The vertical asymptote is $x = -4$

The horizontal asymptote is $y = 0$

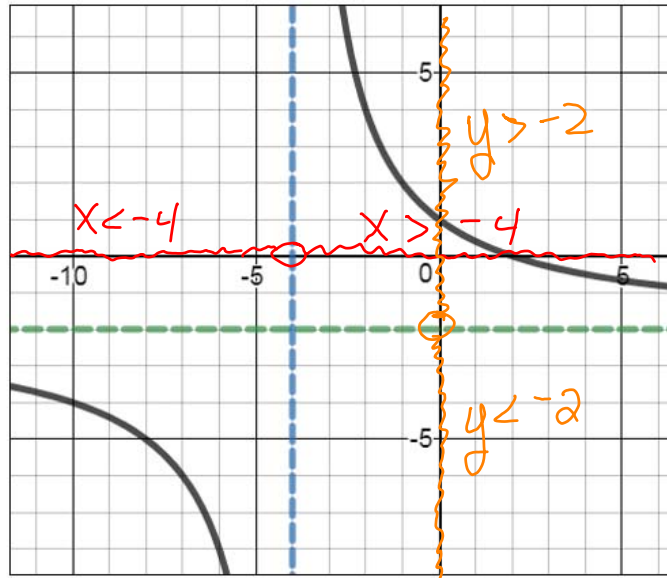


Objective: Determine key features of a rational function from its graph

Concept

The **domain** of a function is the set of all **inputs (values of x)** over which the function is defined.

The **range** of a function is the set of all **outputs (values of y)**.



Domain: $x < -4$ or $x > -4$
 $(-\infty, -4) \cup (-4, \infty)$

Range: $y < -2$ or $y > -2$
 $(-\infty, -2) \cup (-2, \infty)$

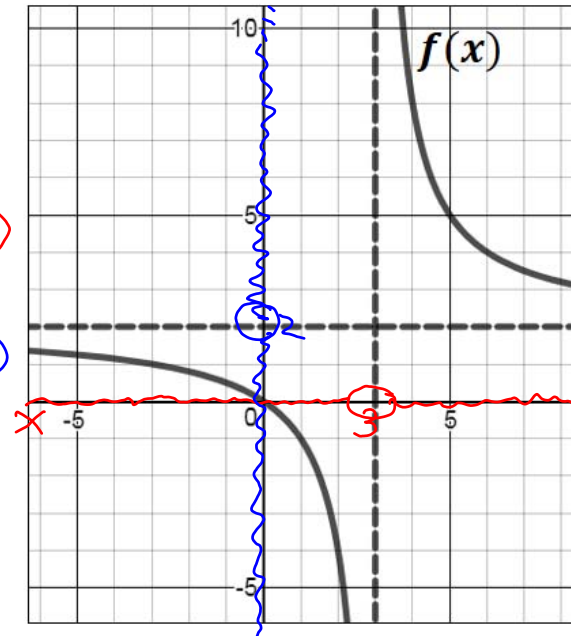


Objective: Determine key features of a rational function from its graph

Ex) Determine the key features for the function $f(x)$.

The domain is $x < 3$ or $x > 3$ / $(-\infty, 3) \cup (3, \infty)$
 (inequality) (interval)

The range is $y < 2$ or $y > 2$ / $(-\infty, 2) \cup (2, \infty)$
 (inequality) (interval)

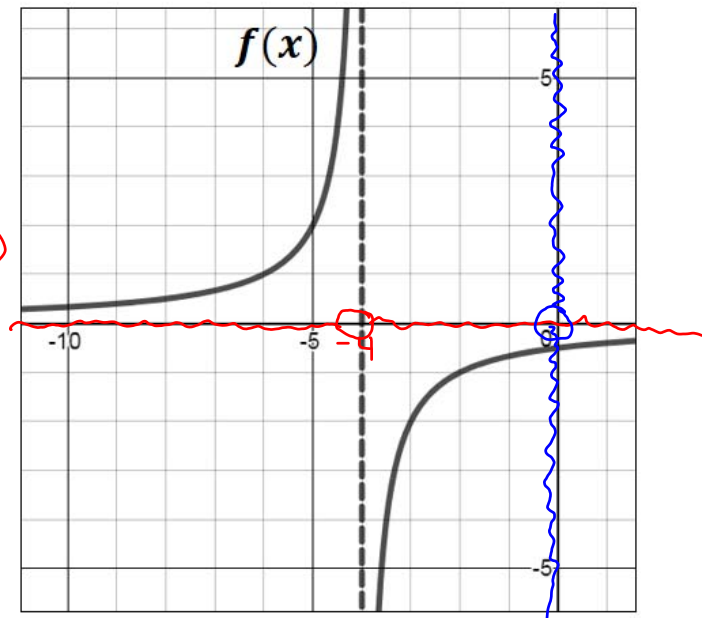


Objective: Determine key features of a rational function from its graph

Ex) Determine the key features for the function $f(x)$.

The domain is $x < -4$ or $x > 4$ / $(-\infty, -4) \cup (-4, \infty)$
 (inequality) (interval)

The range is $y < 0$ or $y > 0$ / $(-\infty, 0) \cup (0, \infty)$
 (inequality) (interval)

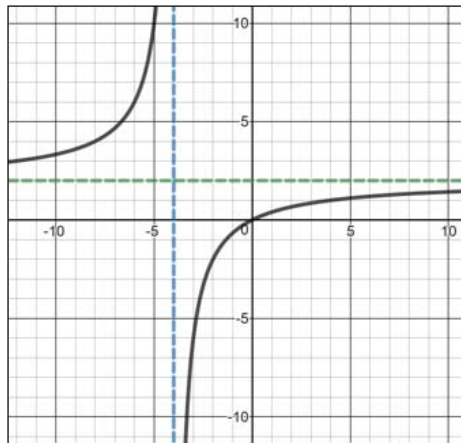


Objective: Determine key features of a rational function from its graph

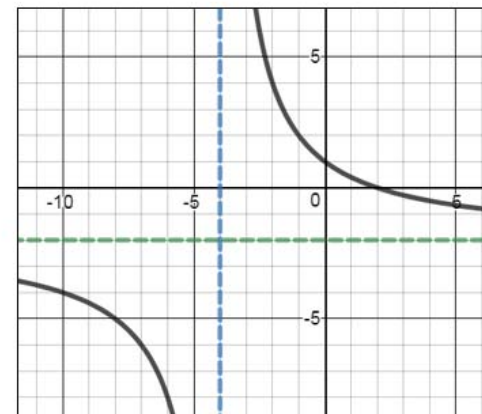
Concept

A function is **increasing** when the **function values increase as the values of the domain increase**. A function can be always increasing or increasing for a specific interval of the domain.

A function is **decreasing** when the **function values decrease as the values of the domain increase**. A function can be always decreasing or decreasing for a specific interval of the domain.



Increasing for: $x < -4$ or $x > -4$
 $(-\infty, -4) \cup (-4, \infty)$

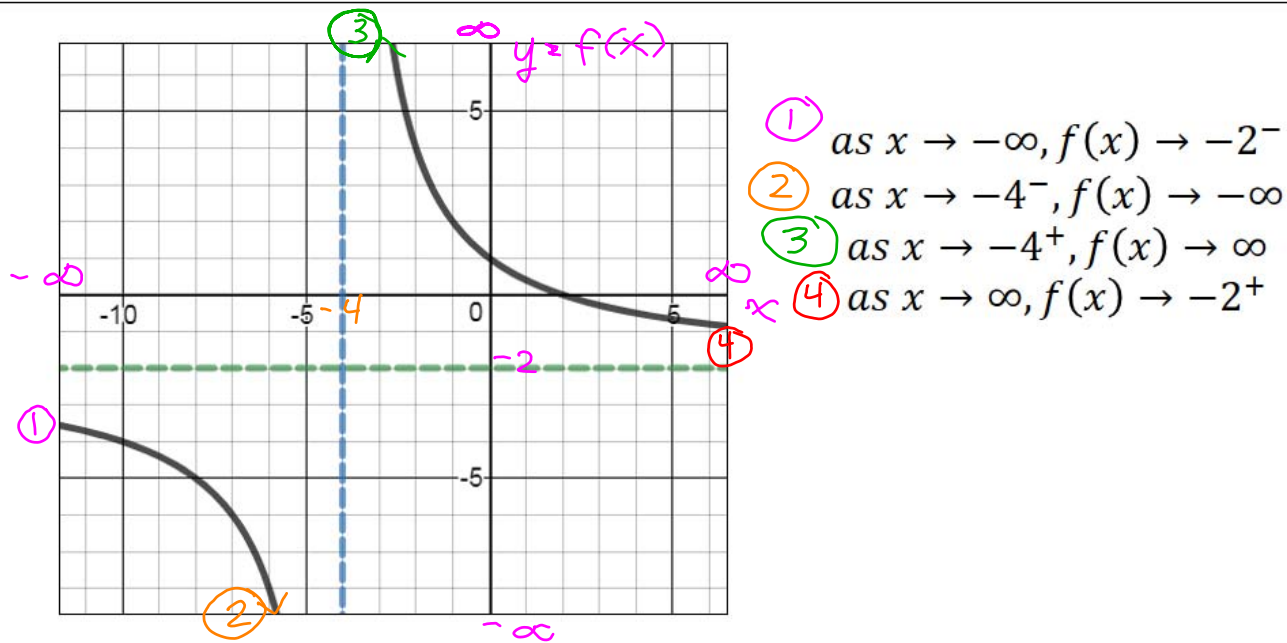


Decreasing for: $x < -4$ or $x > -4$
 $(-\infty, -4) \cup (-4, \infty)$

Objective: Determine key features of a rational function from its graph

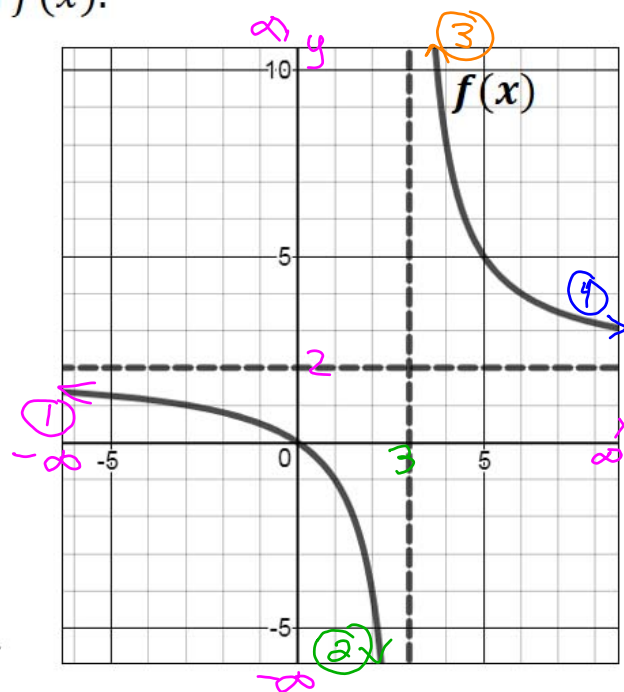
Concept

For a rational function, **end behavior** is a mathematical description of the value the function approaches as x approaches negative infinity, positive infinity, and any value of a vertical asymptote.



Objective: Determine key features of a rational function from its graph

Ex) Determine the key features for the function $f(x)$.



$f(x)$ is increasing/decreasing (circle one) for
 $x < 3$ or $x > 3$ / $(-\infty, 3) \cup (3, \infty)$
 (inequality) (interval)

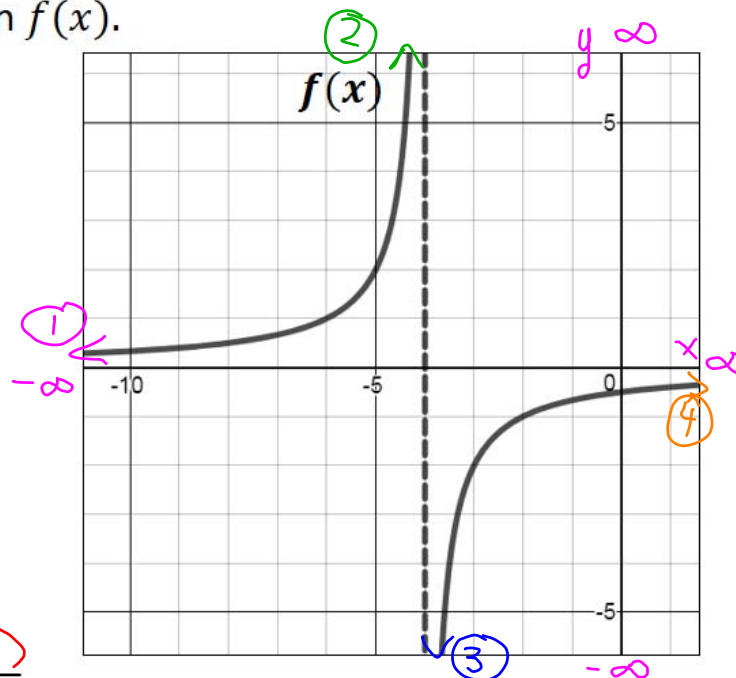
The end behavior of $f(x)$ is

- ① as $x \rightarrow -\infty, f(x) \rightarrow 2^-$
- ② as $x \rightarrow 3^-, f(x) \rightarrow -\infty$
- ③ as $x \rightarrow 3^+, f(x) \rightarrow \infty$
- ④ as $x \rightarrow \infty, f(x) \rightarrow 2^+$



Objective: Determine key features of a rational function from its graph

Ex) Determine the key features for the function $f(x)$.



$f(x)$ is increasing/decreasing (circle one) for
 $x < -4$ or $x > -4$ / $(-\infty, -4) \cup (-4, \infty)$
 (inequality) (interval)

The end behavior of $f(x)$ is

- ① as $x \rightarrow -\infty, f(x) \rightarrow 0^+$
- ② as $x \rightarrow -4^-, f(x) \rightarrow \infty$
- ③ as $x \rightarrow -4^+, f(x) \rightarrow -\infty$
- ④ as $x \rightarrow \infty, f(x) \rightarrow 0^-$