

Objective: See structure in expressions to solve problems.

Concept

Properties of Rational Exponents

For all nonzero real numbers a and b and rational numbers m and n

Words	Numbers	Algebra
Product of Powers Property: to multiply powers with the same base, add the exponents	$12^{\frac{1}{2}} \cdot 12^{\frac{3}{2}} = 12^{\frac{1}{2} + \frac{3}{2}} = 12^2 = 144$	$a^m \cdot a^n = a^{m+n}$
Quotient of Powers Property: to divide powers with the same base, subtract the exponents	$\frac{125^{\frac{2}{3}}}{125^{\frac{1}{3}}} = 125^{\frac{2}{3} - \frac{1}{3}} = 125^{\frac{1}{3}} = 5$	$\frac{a^m}{a^n} = a^{m-n}$ or $\frac{a^m}{a^n} = \frac{1}{a^{n-m}}$
Power of a Power Property: to raise one power to another, multiply the exponents	$\left(8^{\frac{2}{3}}\right)^3 = 8^{\frac{2}{3} \cdot 3} = 8^2 = 64$	$(a^m)^n = a^{m \cdot n}$
Power of a Product Property: to find a power of a product, distribute the exponent	$(16 \cdot 25)^{\frac{1}{2}} = 16^{\frac{1}{2}} \cdot 25^{\frac{1}{2}} = 4 \cdot 5 = 20$	$(ab)^m = a^m b^m$
Power of a Quotient Property: to find a power of a quotient, distribute the exponent	$\left(\frac{16}{81}\right)^{\frac{1}{4}} = \frac{16^{\frac{1}{4}}}{81^{\frac{1}{4}}} = \frac{2}{3}$	$\left(\frac{a}{b}\right)^m = \frac{a^m}{b^m}$



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<p>Negative Exponent Property: moving a power from numerator to denominator or vice versa changes the sign on the exponent</p>	$36^{-\frac{1}{2}} = \frac{1}{36^{\frac{1}{2}}} = \frac{1}{6}$ $\frac{1}{36^{-\frac{1}{2}}} = \frac{36^{\frac{1}{2}}}{1} = \frac{6}{1} = 6$	$a^{-n} = \frac{1}{a^n} \text{ or } \frac{1}{a^{-n}} = a^n$
<p>Zero Exponent Property: any monomial to a power of 0 is equal to 1</p>	$(3)^0 = 1$	$(a)^0 = 1$



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Rewrite the expression in simplest form.

$$\frac{x^5 y^{-1} z}{x^8 y^6 z^{-3}}$$

$$\frac{x^5 z \cdot z^3}{x^8 y^6 y^1} = \frac{z^{1+3}}{x^{8-5} y^{6+1}} = \boxed{\frac{z^4}{x^3 y^7}}$$



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$$2^{-3} = ?$$

$$\frac{1}{2^3} = \boxed{\frac{1}{8}}$$



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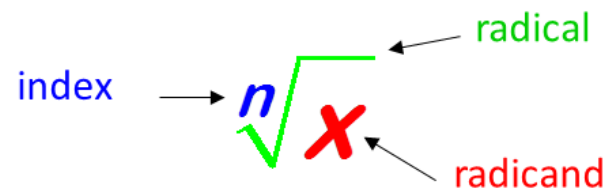
Concept

Rational and irrational numbers expressed in radical form can also be expressed with fractional exponents. When the number has a fractional exponent, it is said to be in [rational exponent](#) form.

$$b^{\frac{1}{n}} = \sqrt[n]{b}$$

and

$$b^{\frac{p}{n}} = \sqrt[n]{b^p} \text{ or } b^{\frac{p}{n}} = (\sqrt[n]{b})^p$$



A diagram illustrating the components of a radical expression. It shows a radical symbol with a blue 'n' as the index and a red 'x' as the radicand. Three arrows point to these parts: a blue arrow from the word 'index' to the 'n', a green arrow from the word 'radical' to the radical symbol itself, and a red arrow from the word 'radicand' to the 'x'.

$$\text{index} \rightarrow n \sqrt{\text{radical } x \text{ radicand}}$$

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Simplify each numerical value as much as possible.

$$\left(\frac{32}{243}\right)^{\frac{2}{5}}$$

$$(512)^{-\frac{2}{3}}$$

$$\frac{(\sqrt[5]{32})^2}{(\sqrt[5]{243})^2} = \frac{(2)^2}{(3)^2} = \boxed{\frac{4}{9}}$$

$$(\sqrt[3]{512})^{-2} = (8)^{-2} = \frac{1}{8^2} = \boxed{\frac{1}{64}}$$

$$\frac{1}{512^{\frac{2}{3}}} = \frac{1}{(\sqrt[3]{512})^2} = \frac{1}{8^2} = \frac{1}{64}$$

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Concept

The Quadratic Function

standard form

$$f(x) = ax^2 + bx + c$$

• vertex = $\left(\frac{-b}{2a}, f\left(\frac{-b}{2a}\right)\right)$

Find the vertex and state whether it is a maximum or minimum.

$$g(x) = 2(x-1)^2 + 2$$

$$\text{vertex} = (h, k) = (1, 2)$$

$a = 2$, no reflection

vertex: (1, 2), minimum

$$f(x) = -x^2 + 6x + 3$$

$$x = -\frac{b}{2a} = -\frac{6}{2(-1)} = \frac{-6}{-2} = 3$$

$$y = -1(3)^2 + 6(3) + 3 = 12$$

$a = -1 \rightarrow x$ -axis reflection

vertex: (3, 12), maximum

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Find the zeros of the function.

$$p(x) = -2x^2 + 4x + 6$$

$$0 = -2x^2 + 4x + 6$$

$$0 = -2(x^2 - 2x - 3)$$

$$0 = -2(x-3)(x+1)$$

$$-2 \neq 0, \quad x-3=0, \quad x+1=0$$

$$x=3 \quad x=-1$$

zeros: $-1, 3$



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Find the zeros of the function.

$$g(x) = x^3 - 7x^2 - 8x$$

$$0 = x^3 - 7x^2 - 8x$$

$$0 = x(x^2 - 7x - 8)$$

$$0 = x(x - 8)(x + 1)$$

$$x = 0, \quad x - 8 = 0, \quad x + 1 = 0$$

$$x = 8 \quad x = -1$$

zeros: $-1, 0, 8$



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Rewrite $x^2 - 8x + 2$ in the form: $(x + \square)^2 + \square$
 perfect square trinomial

$$(x^2 - 8x + \frac{16}{2}) + 2 - \frac{16}{2}$$

$(-\frac{8}{2})^2$
 $(-4)^2$

$$(x - 4)(x - 4)$$

$$(x - 4)^2 - 14$$

$$(x + (-4))^2 + (-14)$$

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What is the factored form of $x^2 - 121y^2$?

$$(x)^2 - (11y)^2$$

$$(x + 11y)(x - 11y)$$



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Rewrite the expression in simplest form.

$$\frac{x^2 - 2x - 8}{x^2 - 16}$$

$$\frac{\cancel{(x-4)}(x+2)}{\cancel{(x-4)}(x+4)} = \boxed{\frac{x+2}{x+4}}$$

What are the excluded x values of the expression? Explain your reasoning.

The excluded x values are -4 and 4 because they make the denominator of the original expression equal to 0 .

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Which of the following are equivalent to the given expression?

$$\underline{(x + 6)^2} - \underline{(x - 2)} \underline{(x + 6)}$$

A) $8x + 48$

B) $(x + 6) \overset{\text{gcf}}{[(x + 6) - (x - 2)]}$

C) $8(x + 6)$

D) $4(2x + 12)$

They are all equivalent to the given expression: A,B,C, and D.

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What is the simplest form of $(5 - x + 2x^2) - (3x + 7) - (x^2 - 2)$?

$$5 - x + 2x^2 - 3x - 7 - x^2 + 2$$

$$x^2 - 4x$$



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What is the simplest form of $(x^2 x^5 y^3)^3$?

$$(x^{2+5} y^3)^3 \rightarrow (x^7 y^3)^3 \rightarrow x^{7 \cdot 3} y^{3 \cdot 3} \rightarrow \boxed{x^{21} y^9}$$



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What is the simplest form of $\left(\frac{x^8}{x^2}\right)^2$?

$$(x^{8-2})^2 \rightarrow (x^6)^2 \rightarrow x^{6 \cdot 2} \rightarrow \boxed{x^{12}}$$



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Which of the following equations are true for all values of x ?

$$a) 2^{4x} = 4^{2x} \rightarrow 16^x = 16^x$$

$$b) 6^x = 3^{2x} \rightarrow 6^x = 9^x$$

$$c) 2^{3x} = 8^x \rightarrow 8^x = 8^x$$

$$d) 3^{3x} = 9^x \rightarrow 27^x = 9^x$$

a and c

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Choose the domain for each function.

$f(x) = \sqrt{x-3}$	$x \neq 3$	$x \neq 4$	$x \geq 3$	$x \geq 3,$ $x \neq 4$
$f(x) = \frac{x-3}{x-4}$	$x \neq 3$	$x \neq 4$	$x \geq 3$	$x \geq 3,$ $x \neq 4$
$f(x) = \frac{x-4}{x-3}$	$x \neq 3$	$x \neq 4$	$x \geq 3$	$x \geq 3,$ $x \neq 4$
$f(x) = \frac{\sqrt{x-3}}{x-4}$	$x \neq 3$	$x \neq 4$	$x \geq 3$	$x \geq 3,$ $x \neq 4$